

Take-Home Assignment - Part 2

Theory

OLS Proof:

After reviewing it, wait fifteen minutes and try to write down the OLS Proof of Unbiasedness for yourself (and annotate each transformation – i.e. jot down, what this step does). Highlight where you got stuck and had to revisit the proof; mark in different color where you feel like you don't fully understand the step; mark in a third color where you use $E(u|X)=0$ (or $E(uX)=0$)

Endogeneity

A.) Now redo the proof, but assume $E(u|X) = 0.65$

⇒ What bias do you get?

⇒ Proof your answer by showing it in the proof.

B.) Write down all 4 sources of endogeneity.

C.) Below is a Haiku that describes a situation where endogeneity biased the estimation result. Which source of endogeneity does it refer to?

Haiku: Bias

Regressed hospital visits on mortality.

Found that hospitals kill people.

But Healthy don't go to hospital.

D.) Try to think of 2 (or up to 4 if you want to do one for each source) examples/regressions where an important source of endogeneity is likely to bias an OLS-estimation. Briefly describe it in a few lines. (hint: a Haiku (3 lines with 3-7 words; See below for an example) that describes it).

Regression Exercises

Question E1: Omitted Variables

Generate a 5-dimensional multivariate normal (Y, X1, X2, Z1, Z2). 5347 observations (alternatively use your own data), with bilateral correlations as follows:

Correlations	Y	x1	x2	Z1	Z2
Y	1.0	0.2	0.1	0.35	0.0
x1	0.2	1.0	0.0	0.4	0.0
x2	0.1	0.0	1.0	0.0	0.4
Z1	0.35	0.4	0.0	1.0	0.6
Z2	0.0	0.0	0.4	0.6	1.0

Add a vector of ones (or any other constant)

- 1.) Manually compute the sample covariances for all pairs and the sample variances. Compare the difference between the sample covariances (the matrix you get from your data) and the theoretical Var-Cov Matrix (the matrix above). Is it exactly the same? Is it almost the same?
- 2.) Univariate Regression:
 - a. Use these to obtain the regression coefficient when regressing Y only on X1 (slide set from Intro)
 - b. Use standard regression commands to regress y only on x1. Compare the coefficient.
- 3.) Multivariate Regression on foot
 - a. Next define your data (ones and the two X columns as Matrix X [ignore the Z variables for now])
 - b. Compute $X'X$
 - c. Compute beta-hat for x1 and x2
 - d. Now run the standard regression command
 - e. Compare.
- 4.) Compare your univariate to you multivariate regression
 - a. What would theory predict regarding the difference of the coefficients between between uni and multivariate regression?
 - b. Comparing your results, is the estimated coefficient for X1 the same or different between uni and multivariate?
 - c. Is that exactly what theory predicted? (Why or why not?)
- 5.) Finally: Compute the CEF for $Y|x_1$ (discretize x1 as you see fit).
 - a. Draw and report.
 - b. When you compare points 2, 3 and 4, what do you observe?

P.S. Please try to set a “seed” at 420711 (cf. googling):