

# **The Global Economy II**

Nova SBE – Spring 2023

Miguel Lebre de Freitas, Diogo Lima, Pedro Sousa Coelho

Resit 16/06/2023 – Duration: 1h45

## **I (4.5)**

*Define **three** of the following concepts (3-5 lines each):*

i. GNDI

ii. Trading risk

iii. Overshooting

iv. Exchange rate pass through

v. Peso problem

## **IV (2)**

*In each question, choose one (correct answer: +0.5; wrong answer: -0.125):*

- a. In a 2-period open economy, a temporary output contraction causes: (i) a fall in private consumption; (ii) an improvement in the current account; (iii) a fall in private investment; (iv) all the above.
- b. The relative PPP will fail in the long run in the presence of: (i) transportation costs; (ii) sticky prices; (iii) permanent fiscal changes; (iv) none of the above.
- c. Deviations from uncovered interest rate parity can be explained by: (i) differences between income taxes and taxes on capital gains; (ii) risk aversion; (iii) barriers to capital mobility; (iv) all the above.
- d. Joining a currency area from below the OCA line will be less likely to be self-validating if, all else equal: (i) the country specializes according to comparative advantages; (ii) trade becomes more intra-industry; (iii) labor mobility increases; (iv) none of the above.

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### II (13.5)

Unless otherwise stated, please present the results with, at most, 2 decimal places.

**II.A.** Consider an economy with flexible prices under fixed exchange rate, where money demand is given by:  $m^D = Y/10i$ , being  $i$  is the nominal interest rate. The foreign price level is  $P^* = 2$ , the real interest rate is 25%, both the Fisher principle and PPP hold each moment in time, and full employment output is always reached at  $Y^f = 100$ . Initially, the money supply is constant and equal to  $M = 40$ , and the initial CB holdings of foreign reserves are  $eB_C^* = 24$ .

a) Quantify the initial values for:

(a1) the real money demand

$$m^D = \frac{Y}{10i} = \frac{100}{10 \cdot 0,25} = 40$$

Note:  $e$  is fixed  $\Rightarrow eP^* = P$  [ $P$  is fixed as  $P^*$  is exogenous]  $\Rightarrow \pi = 0\% \Rightarrow i = r = 25\%$

(a2) the price level

$$\frac{M}{P} = m^D \Leftrightarrow \frac{40}{P} = 40 \Leftrightarrow P = 1$$

(a3) the exchange rate

$$\text{By PPP, } eP^* = P \Leftrightarrow e = \frac{P}{P^*} \Leftrightarrow e = \frac{1}{2}$$

The peg is set at  $\bar{e} = 1/2$

(a4) the velocity of money

$$\text{By the Equation of Exchange, } MV = PY \Leftrightarrow 40v = 100 \cdot 1 \Leftrightarrow v = \frac{100}{40} \Leftrightarrow v = 2,5$$

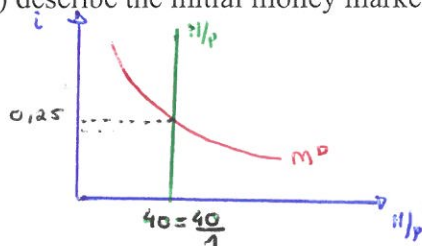
(a5) the central bank's balance sheet

$$M = eB_C^* + B_{CB} \Leftrightarrow 40 = 24 + B_{CB} \Leftrightarrow B_{CB} = 16$$

Then,

A	L
$eB_C^* = 24$	$M = 40$
$B_{CB} = 16$	

(a6) describe the initial money market equilibrium in a graph



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b) Now suppose that there was a one-time productivity surge in our economy, which led to:  $Y' = 125$ . Assuming that the central bank keeps the peg:

(b1) compute the real money demand;

$$m^d = \frac{Y}{10i} = \frac{125}{10 \cdot 0,125} = 50 \quad (\uparrow)$$

No change in  $i$  [follows the same reasoning as in a1]

(b2) find the money supply;

$$\frac{M}{P} = m^d \Leftrightarrow \frac{M}{1} = 50 \Leftrightarrow M = 50 \quad (\uparrow)$$

Note: if the CB keeps the peg ( $\bar{\epsilon}$ ) and  $p^*$  are exogenous,  $P$  cannot change (still equal to 1)

(b3) draw the central bank's balance sheet, explaining how the central bank intervenes.

↳ the CB adjusts  $M$  to keep the peg. This adjustment is fully done with  $eB_{CB}^f$ , as there is no indication that the domestic agents demand more credit.

$$\rightarrow \Delta M = \Delta eB_{CB}^f \Leftrightarrow \Delta eB_{CB}^f = 50 - 40 = 10$$

$$\rightarrow \text{new } eB_{CB}^f = 24 + 10 = 34$$

$$\rightarrow \Delta B_{CB} = 0 \Rightarrow B_{CB} = 16$$

A	L
$eB_{CB}^f = 34$	$M = 50$
$B_{CB} = 16$	

c) Departing from b), assume that unexpectedly the central bank decided to increase domestic bonds by 25% each year to finance reoccurring government deficits, while keeping the peg. Considering that investors are rational and have perfect foresight, describe and quantify:

(c1) The money market equilibrium when the central bank announces the policy and after the attack

(1) Upon announcement

↳ the peg is still kept  $\Rightarrow \bar{\epsilon} \Rightarrow \bar{P} \Rightarrow \pi = 0\% \Rightarrow i = 25\% \Rightarrow m^d = 50$  (equal to  $B_1$ )

↳ Then, as  $P = 1$ ,  $M = 50$ .  $M$  is fixed (to keep the peg, the increase in  $B_{CB}$  will be offset by a decrease in  $eB_{CB}^f \rightarrow$  sterilization)

(2) after the attack

↳ the attack occurs when the price (and the exchange rate) after it are equal to the pre-attack values, meaning that  $P = 1$  still. But the peg breaks and forex collapses to 0, meaning that  $M = B_{CB}$ .

(c2) The central bank balance sheet immediately after the attack

↳ After the attack there are no more foreign reserves.

$$\rightarrow \text{then, } M = B_{CB} = 25$$

A	L
$eB_{CB}^f = 0$	$M = 25$
$B_{CB} = 25$	

$$\rightarrow M_{CB} = B_{CB} \text{ on } = 25\%$$

$$\rightarrow \pi = 4 = 25\%$$

$$\rightarrow i = r + \pi = 25\% + 25\% = 50\%$$

$$\rightarrow m^d = \frac{Y}{10i} = \frac{125}{10 \cdot 0,5} = 25$$

$$\rightarrow \frac{M}{P} = m^d \Leftrightarrow M = P \cdot m^d \Leftrightarrow M = 25$$

(c3) The timing of the regime change. Explain the intuition.

Note: There were other ways to solve this exercise that also received full mark

↳ The attack will occur when agents make no capital gains / losses with it, which implies that  $\Delta P = \Delta \epsilon = 0$

$t=0$

$$B_{CB} = 16$$

$$eB_{CB}^f = 34$$

$$M = 50$$

If we attack:

$$\rightarrow M = B_{CB} = 16$$

$$\rightarrow \frac{M}{P} = m^d \Leftrightarrow \frac{16}{P} = 25 \Leftrightarrow P = 0,64$$

$\rightarrow P \downarrow \Rightarrow$  too early to attack

$t=1$

$$B_{CB} = 16 \cdot 1,25 = 20$$

$$eB_{CB}^f = 34 - \Delta B_{CB} = 30$$

$$M = 50$$

If we attack:

$$\rightarrow M = B_{CB} = 20$$

$$\rightarrow \frac{M}{P} = m^d \Leftrightarrow \frac{20}{P} = 25 \Leftrightarrow P = 0,8$$

$\rightarrow P \downarrow \Rightarrow$  too early to attack

$t=2$

$$B_{CB} = 20 \cdot 1,25 = 25$$

$$eB_{CB}^f = 30 - \Delta B_{CB} = 25$$

$$M = 50$$

If we attack:

$$\rightarrow M = B_{CB} = 25$$

$$\rightarrow \frac{M}{P} = m^d \Leftrightarrow \frac{25}{P} = 25 \Leftrightarrow P = 1$$

$\rightarrow \Delta P = 0 \Rightarrow$  optimal to attack

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**II.B.** Consider an open economy with **sticky** prices under **flexible** exchange rates. In this economy, money supply is equal to  $M = 25$ , money demand is given by  $m^D = \frac{Y}{20i}$ , and full employment output is  $Y_f = 100$ . The interest rate parity holds instantaneously, the foreign interest rate is equal to  $i^* = 0.05$ . The foreign price level is sticky and initially equal to the domestic price level at:  $P = P^* = 1$ . The goods market equilibrium is described by the expression:  $Y = 4(\bar{A} + TB)$ , where  $\bar{A} = 30$ ,  $TB = \bar{X} + 5(\theta - 1)$ ,  $\bar{X} = -5$  and  $\theta = \frac{eP^*}{P}$ .

d) Regarding this initial setting, and assuming that no further changes in the exogenous variables are anticipated:

(d1) Compute the expected exchange rate.

→ The  $E(e)$  is the exchange rate when we are at the LR [ $Y = Y_f = 100$ ]

DD

$$Y = 4(\bar{A} + TB) \Leftrightarrow Y = 4[30 - 5 + 5(\frac{eP^*}{P} - 1)] \Leftrightarrow Y = 4[25 + 5(\frac{e}{P} - 1)] \Leftrightarrow Y = 80 + 20\frac{e}{P}$$

$$Y = 100 \Leftrightarrow 80 + 20\frac{e}{P} = 100 \Leftrightarrow 20\frac{e}{P} = 20 \Leftrightarrow e = P \quad \text{valde for the LR}$$

AA

$$\frac{M}{P} = m^D \Leftrightarrow \frac{M}{P} = \frac{Y}{20i} \Leftrightarrow \frac{P}{M} \frac{Y}{20} = i \Leftrightarrow \frac{P}{M} \frac{Y}{20} = i^* - 1 + \frac{E(e)}{e}$$

$$\text{LR} \Rightarrow \frac{e_{LR}}{25} \frac{100}{20} = 0,05 - 1 + 1 \Leftrightarrow \frac{5}{25} e_{LR} = 0,05 \Leftrightarrow e_{LR} = E(e) = 0,25$$

(d2) Derive the AA and DD curves [Consider that  $E(e) = 1$  if you have not done d1].

DD

Following the reasoning in d1, DD:  $Y = 80 + 20\frac{e}{P}$

Given that  $P = 1$ , DD:  $Y = 80 + 20e$

AA

Following the reasoning in d1,  $\frac{P}{M} \frac{Y}{20} = i^* - 1 + \frac{E(e)}{e} \Leftrightarrow \frac{1}{25} \frac{Y}{20} = -0,95 + \frac{1}{e} \Leftrightarrow$

$$\Leftrightarrow Y = -475 + \frac{125}{e} \quad \text{AA}$$

Note

If  $E(e)$  was considered to be 1, AA:  $Y = -475 + \frac{500}{e}$

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(d3) Use AA and DD to compute the short-run equilibrium, namely the nominal exchange rate (please include, at least, 3 decimal places) and output.

[Tip: the quadratic formula is  $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ ]

SR equilibrium :  $AA_0 = DD_0 \Leftrightarrow$

$$\Leftrightarrow -475 + \frac{125}{e} = 80 + 20e \Leftrightarrow$$

$$\Leftrightarrow -475e + 125 = 80e + 20e^2 \Leftrightarrow$$

$$\Leftrightarrow 20e^2 + 555e - 125 = 0 \Rightarrow$$

$$\Rightarrow e = 0,223 (e > 0) \quad [ \text{If } e(e) = 1, e = 0,873 ]$$

Then,  $y = 80 + 20 \cdot 0,223 = 34,87$

If  $e(e) = 1, y = 97,46$

(d4) Find the trade balance.

$$TB = \bar{x} + s(\theta - 1) = -5 + 5 \left( \frac{0,223 \cdot 1}{1} - 1 \right) = -8,88$$

If  $e(e) = 1, y = -5,635$

(d5) Compute the long-run price level in the absence of policy interventions.

Following the reasoning in d1,  $DD: y = 80 + 20 \frac{e}{p}$

If we are at the LR,  $y = 100 \wedge e(e) = e = 0,25$

Then,  $100 = 80 + 20 \cdot \frac{0,25}{P_{LR}} \Leftrightarrow 20 = \frac{5}{P_{LR}} \Leftrightarrow P_{LR} = 1/4$

In the LR, prices will converge to  $1/4$ .

(d6) Derive the long-run AA & DD curves in the absence of policy interventions.

DD

In the LR, the DD curve will change due to the change in  $p$

$$y = 80 + 20 \frac{e}{p} \text{ with } p = 0,25 \Rightarrow y = 80 + \frac{20}{0,25} e \Leftrightarrow y = 80 + 80e \quad DD_{LR}$$

AA

$$\frac{p}{M} \frac{y}{20} = i^* - 1 + \frac{E(e)}{e} \Leftrightarrow \frac{0,25}{25} \frac{y}{20} = -0,95 + \frac{0,25}{e} \Leftrightarrow y = -1900 + \frac{500}{e} \quad AA_{LR}$$

$\frac{E(e)}{e} = 1$  as we are at the LR

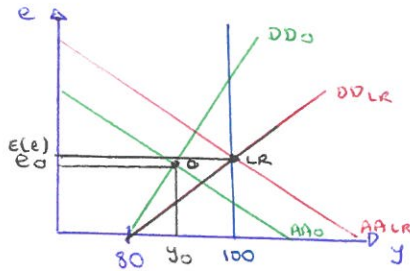
$\hookrightarrow$  The AA curve will change due to the new level of  $p$ .

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(d7) Describe, explaining in detail, the adjustment to the long-run referring to the AA-DD diagram.

$e_0 = 0,223$  or  $0,873$   
 $y_0 = 84,87$  or  $91,46$   
 $E(e) = 0,25$  or  $1$



e) Assume now that the government urged the central bank to **permanently** change the money supply in order to restore full employment:

(e1) Find the required level of the money supply and the new expected exchange rate.

$\rightarrow$  By the DD curve (and knowing that  $y=100$  and  $P=1$ ):  $100 = 80 + 20e \Rightarrow e = 1$   
 The policy drives  $y$  to  $y_F$   $\downarrow$   $P$  will not adjust in the SR  $\downarrow$  the new  $E(e)$  is 1

$\rightarrow$  By the AA curve [with  $y=100$ ,  $P=1$  and  $E(e)=1$ ]:

$$\frac{P}{M} \frac{y}{20} = i^* - 1 + \frac{E(e)}{e} \Rightarrow \frac{1}{M} \frac{100}{20} = 0,05 \Rightarrow \frac{5}{M} = 0,05 \Rightarrow M = 100$$

(e2) Derive the AA & DD curves after the implementation of the policy.

Our goal is to find the SR AA and DD curves.

$\rightarrow$  In the SR, there is no change in  $P \Rightarrow$  same DD curve  $\Rightarrow y = 80 + 20e$

$\rightarrow$  AA changes due to  $\Delta M$  and  $\Delta E(e)$ :

$$\frac{1}{100} \frac{y}{20} = -0,95 + \frac{1}{e} \Rightarrow \frac{y}{2000} = -0,95 + \frac{1}{e} \Rightarrow y = -1900 + \frac{2000}{e}$$

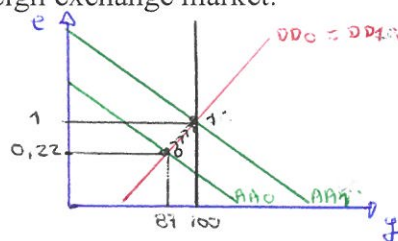
(e3) Describe, explaining in detail, the adjustment process, referring to the AA-DD diagram, the money market, and the foreign exchange market.

### ① AA-DD

$$AA_0: y = -475 + \frac{125}{e}$$

$$DD_0: y = 80 + 20e = DD_1$$

$$AA_1: y = -1900 + \frac{2000}{e}$$



### ② Asset Approach

$$\begin{aligned}
 i_0 &= i^* + \frac{E(e)_0}{e_0} - 1 = 0,05 + \frac{0,25}{0,223} - 1 = 0,18 \\
 i_1 &= i^* + \frac{E(e)_1}{e_1} - 1 = 0,05 + 1 - 1 = 0,05
 \end{aligned}
 \quad \left. \vphantom{\begin{aligned} i_0 \\ i_1 \end{aligned}} \right\} \text{Then, } i \text{ goes down}$$

